Classifying Runtime Performance with SVM

David Eliahu  Shaddi Hasan  Omer Spillinger

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Abstract

We present a machine-learning based technique for the problem of algorithm selection, specifically focusing on algorithms for dense matrix multiplication (DMM). Dense matrix multiplication is a core part of many high-performance computing and machine learning algorithms, but the performance of DMM algorithms can vary significantly based on their input and the performance characteristics of each particular machine. We model machine performance using support vector machines and show that only a small sample of possible inputs is sufficient to determine the best choice of algorithm over a wide range of possible inputs and even over different machines (by training a model per machine). We find that by using this classifier-based approach and choosing the best algorithm to use at runtime, we are able to achieve at least a 0.5% and as much as a 28% increase in performance over choosing a single algorithm a priori.

1 Introduction

Algorithm designers produce an ever-increasing set of techniques for solving an ever-wider set of problems. Indeed, algorithm selection itself has become a challenging problem, particularly in fields where performance is critical such as machine learning and scientific computing. The factors that influence algorithm performance are extremely complicated, and understanding how an algorithm will perform given an input and a particular machine can require extensive domain expertise. Performance can vary significantly from system to system due to differences in factors such as memory hierarchy, machine architecture, utilization, and so on. This problem is even more pronounced on virtualized infrastructure: the application developer really has no way of knowing how the underlying hardware will perform, or even if her application will always be running on the same hardware (e.g., due to virtual machine migration).

All this made us ask ourselves: how can we predict the optimal algorithm to use in a given situation? Being able to do so would be a significant benefit to developers; such a technique could be incorporated into libraries so that developers could write software oblivious to the underlying algorithmic implementation, confident that the library would choose the proper algorithm.

One solution to this problem would be to develop a model of machine performance and analytically determine the best algorithm to use for a given input. Clearly, this approach wouldn’t scale—the model would be enormously complex, and would need to be developed for every combination of machine and algorithm.

One could also take an empirical approach: simply measure how algorithms perform on a given machine under different inputs. A naïve solution would be to exhaustively search the space of possible inputs; this is intractable in the general case, and even in situations where the range of possible inputs is finite, exhaustive search is time consuming.

The complexity of performance classification lends itself to a machine learning approach. Rather than building a complex model of machine performance, we can train a classifier on a set of training examples to predict the best algorithm to use. In contrast to exhaustive search, a classifier-based approach need not explore a large portion of the search space. The user can make an explicit tradeoff between classifier accuracy and training time.

We take this classifier-based approach in our project. In this work, we focus on dense matrix multiplication (DMM). We chose this problem for several reasons. First, DMM is an important step in many HPC and machine learning tasks, and it often represents the computational performance bottleneck for those tasks. Thus, even relatively small performance gains for DMM can translate to real savings for large tasks. Second, a plethora of algorithms for DMM exist in the literature. Two of the authors have developed a communication-avoiding algorithm for DMM
called CARMA [1]; CARMA's approach is substantially different than the industry-standard algorithm MKL [2], making it likely that it would have different performance properties across different machines. Finally, DMM is easily parameterizable—in general, performance is dictated by the dimensions of the input matrices.

We perform classification using a support vector machine [3]. We evaluate our classifier on a set of multiplications of matrices ranging in size from 64 x 64 to 3250 x 3250—a state space of over 32 billion possible inputs. We find that our classifier achieves good results across multiple machines, with F1 scores ranging from 0.75 to 0.88, and that training on only a few hundred points is usually sufficient to achieve this level of accuracy. Finally, using our approach we observe performance increases of up to 28% versus choosing an algorithm a priori.

The remainder of the paper is organized as follows. We first discuss our dataset and its generation. We then describe our approach towards evaluation and analysis. In section 5 we describe our results before considering future directions and concluding.

2 Related Work

The idea of using machine learning techniques to improve performance on complex architectures is not new. Increasingly complicated machine architectures and compilers motivate a shift from analytical to empirical approaches. However, most literature on this topic focuses on auto-tuning for templated-code optimization problems using regression models [4]. Our approach is not limited to auto-tuning within an algorithm template, as we are more interested in performance variations between linear algebra algorithms and their communication-avoiding counterparts.

Another relevant topic of research is the improvement of exhaustive search techniques. Heuristics may be used for terminating exhaustive search early if near-optimal implementations are found. In addition, run-time decision rules can be used to select fast implementations based on run-time input [5] [6]. Although this approach is similar to ours, it explores a two-dimensional rather than three-dimensional space and tunes parameters within a single algorithmic template while we focus on algorithm selection.

3 Data

Our project takes an empirical approach to the algorithm selection problem. Thus, our first step is to collect data for analysis.

3.1 Generating Data

We featurize matrix multiplications based on the dimensions of the input matrices: M, K, and N. These features represent the size of each dimension of a matrix multiplication of the form $M \times K \times K \times N$. We generated random dense matrices with real-valued floating point numbers ranging in size from $64 \times 64$ to $3250 \times 3250$. We varied each dimension in 10 evenly-spaced increments across that range. Note that this means we generated a range of rectangular matrices, not just square ones.

This step results in 1000 possible matrix multiplications (i.e., combinations of M, K, and N). We then run each of these matrix multiplications using both of our algorithms under test (MKL and CARMA) and record the performance of each multiplication in gigaflops/second (Gflops). We repeat each multiplication three times and compare the max performance for each algorithm. This constitutes a single datapoint for our classifier: a tuple (M,K,N) and a binary label representing which algorithm ran faster. Finally, we performed this process on three separate machines with different architectures, for a total of 18,000 matrix multiplications and 3,000 training points. The machines we used are shown in Table 1.

To multiply the matrices, we wrote a custom matrix multiplication program in C. Our program allocates three matrices (A, B, and C) and initializes them with random floats between -1 and 1. We then perform a single matrix multiplication to warm-up the processor, clear the cache, and multiply the random matrices we generated. To ensure that the matrix multiplication operation takes sufficient time to be accurately measured, we perform as many multiplications as necessary so that the total time of all multiplications is at least 0.2 seconds. We then divide the total time by
<table>
<thead>
<tr>
<th>Machine</th>
<th>Cores</th>
<th>CPU Type</th>
<th>Memory</th>
</tr>
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<tbody>
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<td>Intel Xeon X7560</td>
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</tr>
<tr>
<td>Hopper</td>
<td>24</td>
<td>AMD “MagnyCours”</td>
<td>32GB</td>
</tr>
<tr>
<td>Sandy</td>
<td>8</td>
<td>Intel i7-2600</td>
<td>16GB</td>
</tr>
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Table 1: Machines used for evaluation.

the number of multiplications to calculate the time for a single matrix multiplication. To compute Gflops, we divide $2^{-9} \times m \times k \times n^1$ by the time for a single multiplication.

3.2 Limitations

Our data has a few limitations. First and foremost, our largest matrix is $3250 \times 3250$. While this is a large matrix, it still fits in memory on all our machines; we did not explore extremely large matrix sizes, though we believe our technique is general enough to scale to those as well. Secondly, some of the machines we used to generate data were shared machines. As a result, our performance would sometimes fluctuate significantly between trials. To accurately evaluate how fast the multiplication would run in an ideal environment, we took the max Gflops measurement over three trials (due to time constraints, we were unable to perform more than three measurements per datapoint per machine). Nevertheless, our classification results were strong, so we do not believe that the remaining variability after maxing over three trials significantly impacted our evaluation or the significance of our results.

4 Classification

Intuitively, we expected the regions in which each algorithm performed better to be highly nonlinear. As a result, we chose to use a support vector machine for classification, as these are known to have good performance for nonlinear classification [3]. Specifically, we used MATLAB’s [7] implementation of SVM. We chose to compare two kernels, the Gaussian radial basis function (RBF) [8] and the multilayer perceptron (MLP) [9].

As described in section 3.1, we featurized DMM by using the sizes of the input matrices: M, K, and N. The output of our classifier is the algorithm that performs better for a given tuple (M, K, N). The classifier only considers the binary training data—we do not take into account how much better an algorithm performs at each point; we leave this weighted classification to future work.

4.1 Training

We trained our classifier on each of our three testing machines. Our results, shown in Figure 1, were surprising. While we expected some machine-to-machine variation, the regions where each algorithm performs better are substantially different across machines. Indeed, Emerald and Sandy have diametrically opposed training results. We do not have a theoretical model to explain this variation, which further illustrates the value of our empirical machine learning approach. This is a key result: techniques that do not consider per-machine variation are certain to use the wrong algorithm in many cases. We also note that the regions of optimal performance for each algorithm are in fact nonlinear.

Another surprising result of our training was the fact that CARMA performed well for such large regions. CARMA’s developers had designed it for multiplication of “long, skinny” matrices, and it outperformed MKL for those on all three of our machines. However, its strong performance for other types of matrices was unexpected, and will be analyzed in the future.

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1Each entry of the resulting $M \times N$ matrix requires K multiply and K add operations, hence this total for Gflops.
4.2 Classifying

In order to evaluate our classifier, we needed to generate random datapoints for testing. We randomly generated values for $M$, $K$, and $N$ within our training space\(^2\) and replicated our data-collecting procedure to time the multiplications and record which algorithm ran faster. After gathering this test data, we removed the true class labels and values for $M$, $K$, and $N$ through our classifier (once per machine for each kernel). Given the true and predicted label for each testing datapoint, we now had enough information to evaluate our classifier. See Figure 2 for the results of this procedure.

It’s worth noting that the majority of incorrect classifications occur on or near the decision boundaries our classifier generated. This is due to the fact that along these decision boundaries, the performance of MKL and CARMA is comparable. On any given trial, CARMA may slightly outperform MKL, or MKL may marginally beat CARMA. Therefore, the class that our classifier assigns to datapoints along a decision boundary may not match the given instance of performance data that we gathered, even though the actual performance difference is relatively minor.

To better visualize this phenomenon, we simplified the problem by reducing it to a two-dimensional classification problem (Figure 3). By only considering datapoints where $K = N$, we were able to train a 2D classifier to better visualize the decision boundary. Note that in this slice, incorrect decisions occur near the boundary determined by the SVM.

On average, the performance loss resulting from an incorrect classification is only 9.6%, supporting the observation that the majority of these misclassifications occur along decision boundaries where CARMA’s and MKL’s performance are comparable.

5 Evaluation

We used our training data to develop a performance model for each machine. Note that the performance model is the trained SVM itself, and only considers the end-to-end performance of the training data.

5.1 Classifier Performance

We evaluated the performance of our classifier on each machine according to the using F1 scores (see Table 2). Our classifier performs best on Hopper, which yields an F1 score of 0.88 (with the RBF kernel). On all three machines, the RBF kernel outperforms the MLP kernel.

In order to measure how many datapoints are required to train an accurate classifier, we explored the effects of reducing the size of our training set. In this experiment, we randomly selected X% of our original 1000 training points,\(^{2}\)We did not explicitly prevent overlap in sizes between our training sets and our randomly-generated testing set, given the vast size of the space under consideration (over 32 billion combinations) any such overlap was minimal.
Figure 2: Testing results for each of our three machines, for each kernel (RBF and MLP). Blue dots represent datapoints where our classifier correctly predicted which algorithm was faster, and orange dots represent incorrect classifications. Note that the RBF kernel outperforms the MLP kernel on all machines (most significantly on Emerald and Sandy).

for X ranging from 1% to 100%. After training our classifier with this random X% subset of our training data, we measured the resulting F1 score on the test data. See Figure 4.

Of course, the number of training points required to build an accurate model will vary widely by machine and algorithm. As shown in Figure 4, although Sandy and Hopper require fewer than 500 datapoints to achieve a maximal F1 score, Emerald requires more than 1000. This is due to the fact that performance patterns on Emerald are more complex. We don’t have a theoretical model to understand this complexity, further validating the value our empirical approach.

5.2 Application Performance

We also performed tests to quantify the benefit of using our algorithm selection technique. How much do we gain by using our classifier to select the optimal algorithm? It depends on the machine, as well as what algorithm would have been chosen otherwise. For example, using our classifier on Emerald yields an 11.3% average speedup over using only CARMA, and a 5.7% speedup over using just MKL (this includes the penalties of misclassifications). On Hopper, our classifier enjoys a healthy 28.0% gain over using MKL only. For complete results, see Table 3.

6 Future Work

The input used to train the SVM was binary: if CARMA’s performance was superior to MKL’s performance for a given set of matrix dimensions, the datapoint was given with the CARMA label (and vice versa for MKL). We aim to explore techniques that account for the magnitude of the difference between the two algorithms’ performances. In other words, datapoints for which one algorithm was significantly faster should be weighted more heavily in our
performance model. Performance gains achieved by correctly selecting the faster algorithm are a more important metric for this work than a high overall classification accuracy.

In this project, we examined dense matrix multiplication on three different shared-memory machines. However, the approach of using SVM to partition a feature space based on algorithm performance patterns can be generalized to a wide variety of other algorithms and architectures. We aim to evaluate additional linear algebra algorithms such as QR decomposition and sparse matrix multiplication. Furthermore, we are interested in gathering data on distributed-memory machines in which higher communication costs magnify the performance gains that can be achieved by communication-avoiding algorithms such as CARMA.

Finally, algorithm selection could be incorporated into machine learning as well as scientific computing frameworks. After gathering sufficient training data, the framework could select the optimal algorithm for a given set of input parameters at runtime. The number of samples required for convergence in the dense matrix multiplication case that we explored is orders of magnitude smaller than the size of the feature space (Figure /reffig:convergence). The framework would only classify input parameters above a certain threshold because the overhead of classification cannot be justified for all cases.

7 Conclusion

In this project, we’ve tackled the problem of algorithm selection for HPC and machine learning problems, specifically focusing on dense matrix multiplication. This problem is challenging due to the complexity of analyzing machine
Figure 4: F1 convergence on each machine (using the RBF kernel). Sandy and Hopper require fewer than 500 datapoints to generate accurate performance models, while Emerald requires more than 1000 (due to Emerald’s more complicated performance patterns).

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<thead>
<tr>
<th>Machine</th>
<th>Selection vs CARMA Only</th>
<th>Selection vs MKL Only</th>
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<tbody>
<tr>
<td>Emerald</td>
<td>11.3%</td>
<td>5.7%</td>
</tr>
<tr>
<td>Hopper</td>
<td>2.2%</td>
<td>28.0%</td>
</tr>
<tr>
<td>Sandy</td>
<td>4.4%</td>
<td>0.9%</td>
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Table 3: Runtime performance gains of our algorithm selector vs running a single algorithm.

performance a priori and due to per-machine variation in algorithm performance, the latter of which was dramatically reflected in our training results. We found that using a support vector machine to classify the space of inputs between multiple choices of algorithms can yield good results, with F1 scores as high as 0.88 on one of our testing machines. Moreover, achieving that level of accuracy requires a small training set—only a few hundred data points.

We believe this technique has promise for improving the performance of real applications. The status quo requires developers to think carefully about the machines and data their applications will use, analyze the expected performance, and then choose their algorithm appropriately, hoping they’ve made the right choice for all time. This need not be the case: we’ve demonstrated that our approach is feasible and in general improves performance over the status quo, with up to 28% increase in performance in the best case.

References


